

University of Utah
Math 1220, Fall 2007
Name:

Solutions

Quiz # 2

Time: 15 minutes

Please try to carefully explain the steps leading to your solutions.

Part 1: (10 points) Evaluate the integral:

$$\int \frac{1}{4x^2 + 2} dx$$

We write this as $\int \frac{1}{u^2+1} du$ (which we know how to integrate) by using the substitution: $\begin{cases} u = \sqrt{2}x \\ du = \sqrt{2} dx \end{cases}$

$$\int \frac{1}{4x^2+2} dx = \frac{1}{2} \int \frac{1}{2x^2+1} dx \stackrel{\downarrow}{=} \frac{1}{2\sqrt{2}} \int \frac{1}{u^2+1} du = \frac{1}{2\sqrt{2}} \tan^{-1} u + C$$
$$= \frac{1}{2\sqrt{2}} \tan^{-1}(\sqrt{2}x) + C$$

Part 2: (10 points) Find the derivative of the function $f(x) = (\cos x)^x$. Note that this function is only defined on intervals where $\cos x > 0$.

We start by writing: $f(x) = e^{\ln(\cos x) \cdot x}$

which we differentiate by the chain rule.

We will need: $[\ln(\cos x)]' = \frac{1}{\cos x} \cdot (-\sin x) = -\tan x$ (chain rule)

$[\ln(\cos x) \cdot x]' = -\tan x \cdot x + \ln(\cos x)$ (product rule)

Therefore: $f'(x) = [e^{\ln(\cos x) \cdot x}]' = (-\tan x \cdot x + \ln(\cos x)) \cdot e^{\ln(\cos x) \cdot x}$