

> # Sample Problem 10

> # answer check part (a)

> f:=t\*exp(2\*t)+2\*t\*sin(3\*t)+3\*exp(-t)\*cos(4\*t);

$$f := t e^{2t} + 2 t \sin(3 t) + 3 e^{-t} \cos(4 t)$$

(1)

> with(inttrans): # load laplace package

> laplace(f,t,s);

$$\frac{1}{(s-2)^2} + \frac{12s}{(s^2+9)^2} + \frac{3}{2(s+1-4I)} + \frac{3}{2(s+1+4I)}$$

(2)

> # The last two fractions simplify to 3(s+1)/((s+1)^2+16).

> # answer check part (b)

> F:=16/(s^2+4)+(s+1)/(s^2-2\*s+10)+2/(s^2+16);

$$F := \frac{16}{s^2+4} + \frac{s+1}{s^2-2s+10} + \frac{2}{s^2+16}$$

(3)

> invlaplace(F,s,t);

$$8 \sin(2 t) + \frac{1}{2} \sin(4 t) + \frac{1}{3} e^t (3 \cos(3 t) + 2 \sin(3 t))$$

(4)

> # answer check part (c)

> de:=diff(x(t),t,t)+256\*x(t)=1;ic:=x(0)=1,D(x)(0)=0;

$$de := \frac{d^2}{dt^2} x(t) + 256 x(t) = 1$$

$$ic := x(0) = 1, D(x)(0) = 0$$

(5)

> dsolve([de,ic],x(t));

$$x(t) = \frac{1}{256} + \frac{255}{256} \cos(16 t)$$

(6)

> # answer check part (c), partial fractions

> convert((s^2+1)/(s\*(s^2+256)),parfrac,s);

$$\frac{255}{256} \frac{s}{s^2+256} + \frac{1}{256 s}$$

(7)