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> # Quiz 11 solutions
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> # Problem 1
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> de:=-diff(u(t),t,t) = diff(X(t),t,t) + 16*diff(X(t),t) + 80* X(t)
;
> X:=t->10*cos(3*t);
> dsolve(de,u(t));subs(_C1=0,_C2=0,%);
```

$$de := - \left( \frac{d^2}{dt^2} u(t) \right) = \frac{d^2}{dt^2} X(t) + 16 \left( \frac{d}{dt} X(t) \right) + 80 X(t)$$

$$X := t \rightarrow 10 \cos(3 t)$$

$$u(t) = \frac{710}{9} \cos(3 t) - \frac{160}{3} \sin(3 t) + \_C1 t + \_C2$$

$$u(t) = \frac{710}{9} \cos(3 t) - \frac{160}{3} \sin(3 t) \quad (1)$$

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> # answer check problem 2(a)
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```
> f:=3*(t+1)^2*exp(2*t)+2*exp(t)*sin(3*t);
> with(inttrans): # load laplace package
> laplace(f,t,s);
```

$$f := 3 (t+1)^2 e^{2t} + 2 e^t \sin(3 t)$$

$$\frac{3 (s^4 - 2 s^3 + 4 s^2 + 4)}{(s-2)^3 ((s-1)^2 + 9)} \quad (2)$$

```
> convert(%,parfrac,s);
```

$$\frac{6}{s^2 - 2 s + 10} + \frac{6}{(s-2)^2} + \frac{6}{(s-2)^3} + \frac{3}{s-2} \quad (3)$$

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> # answer check problem 2(b)
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> F:=4*s/(s^2+4)+(s-1)/(s^2-2*s+5);
> invlaplace(F,s,t);
```

$$F := \frac{4 s}{s^2 + 4} + \frac{s-1}{s^2 - 2 s + 5}$$

$$\cos(2 t) (4 + e^t) \quad (4)$$

```
> # answer check problem 2(c)
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```
> x:='x':de:=diff(x(t),t,t)+2*diff(x(t),t)+5*x(t)=exp(t);
ic:=x(0)=0,D(x)(0)=1;
> dsolve([de,ic],x(t));
```

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> # answer check problem 2(c), partial fractions
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$$de := \frac{d^2}{dt^2} x(t) + 2 \left( \frac{d}{dt} x(t) \right) + 5 x(t) = e^t$$

$$ic := x(0) = 0, D(x)(0) = 1$$

$$x(t) = \frac{3}{8} e^{-t} \sin(2 t) - \frac{1}{8} e^{-t} \cos(2 t) + \frac{1}{8} e^t \quad (5)$$

```
> convert((s^2-s+1)/((s-1)*(s^2+2*s+5)),parfrac,s);
```

[

$$\frac{1}{8} \frac{7s-3}{s^2+2s+5} + \frac{1}{8(s-1)}$$

**(6)**