## Population and Sample

- Researchers often want to answer questions about some large group of individuals (this group is called the population)
- Often the researchers cannot measure (or survey) all individuals in the population, so they measure a subset of individuals that is chosen to represent the entire population (this subset is called a sample)
- The researchers then use statistical techniques to make conclusions about the population based on the sample



## Voluntary Response

- Advice columnist Ann Landers asked her readers, "If you had it to do over again, would you have children?"
- A few weeks later, her column was headlined: " $70 \%$ OF PARENTS SAY KIDS NOT WORTH IT."
- The people who responded felt strongly enough to take the trouble to write Ann Landers. Their letters showed that many of them were angry at their children.
- These people don't fairly represent all parents.
- A statistically designed opinion poll on the same issue a few months later found that $91 \%$ of parents would have children again.


## Convenience Sampling

- Sampling mice from a large cage to study how a drug affects physical activity
- lab assistant reaches into the cage to select the mice one at a time until 10 are chosen
-Which mice will likely be chosen? - could this sample yield biased results?


## Simple Random Sampling

- Each individual in the population has the same chance of being chosen for the sample
- Each group of individuals (in the population) of the required size ( $n$ ) has the same chance of being the sample actually selected
- Random selection:
- "drawing names out of a hat"
- table of random digits
- computer software


## Table of Random Digits

- Table B on pg. 692 of text
- each entry is equally likely to be any of the 10 digits 0 through 9
- entries are independent of each other (knowledge of one entry gives no information about any other entries)
- each pair of entries is equally likely to be any of the 100 pairs $00,01, \ldots, 99$
- each triple of entries is equally likely to be any of the 1000 values $000,001, \ldots, 999$


## Probability Sample

- a sample chosen by chance
- a SRS gives each member of the population an equal chance to be selected


Stratified Random Sample Example

Suppose a university has the following student demographics:

Undergraduate Graduate First Professional Specia
$55 \% \quad 20 \%$ 20\%

A stratified random sample of 100 students could be chosen as follows: select a SRS of 55 undergraduates, a SRS of 20 graduates, a SRS of 5 first professional students, and a SRS of 20 special students; combine these 100 students.


## Choosing a Simple Random Sample (SRS)

STEP 1: Label each individual in the population

STEP 2: Use Table B to select labels at random


## Stratified Random Sample

- first divide the population into groups of similar individuals, called strata
- second, choose a separate SRS in each stratum
third, combine these SRSs to form the full sample



## Multistage Sample

- several stages of sampling are carried out
- useful for large-scale sample surveys
- samples at each stage may be SRSs, but are often stratified
- stages may involve other random sampling techniques as well (cluster, systematic, random digit dialing, ...)



## Cautions about Sample Surveys

- Undercoverage
- some individuals or groups in the population are left out of the process of choosing the sample
- Nonresponse
- individuals chosen for the sample cannot be contacted or refuse to cooperate/respond


## - Response bias

- behavior of respondent or interviewer may lead to inaccurate answers or measurements
- Wording of questions
- confusing or leading (biased) questions; words with



## Response Bias

- A door-to-door survey is being conducted to determine drug use (past or present) of members of the community. Respondents may give socially acceptable answers (maybe not the truth!)
- For this survey on drug use, would it matter if a police officer is conducting the interview? (bias from interviewer)



## Wording of Questions

A newsletter distributed by a politician to his constituents gave the results of a "nationwide survey on Americans' attitudes about a variety of educational issues." One of the questions asked was, "Should your legislature adopt a policy to assist children in failing schools to opt out of that school and attend an alternative school--public, private, or parochial--of the parents' choosing?" From the wording of this question, can you speculate on what answer was desired? Explain.


## Nonresponse

- Advice columnist Ann Landers asked her readers, "If you had it to do over again, would you have children?"
- A few weeks later, her column was headlined: " $70 \%$ OF PARENTS SAY KIDS NOT WORTH IT."
- The people who responded felt strongly enough to take the trouble to write Ann Landers. Their letters showed that many of them were angry at their children.
- These people don't fairly represent all parents.
- A statistically designed opinion poll on the same issue a few months later found that $91 \%$ of parents would have children again.



## Response Bias

Asking the Uninformed
Washington Post National Weekly Edition (April 10-16, 1995, p. 36)

- A 1978 poll done in Cincinnati asked people whether they "favored or opposed repealing the 1975 Public Affairs Act."
- There was no such act!
- About one third of those asked expressed an opinion about it.



## Wording: Deliberate Bias

- "If you found a wallet with $\$ 20$ in it, would you return the money?"
- "If you found a wallet with $\$ 20$ in it, would you do the right thing and return the money?"



## Wording: Unintentional Bias

- "I have taught several students over the past few years."
- How many students do you think I have taught?
- How many years am I referring to?
- "Over the past few days, how many servings of fruit have you eaten?"
- How many days are you considering?
- What constitutes a serving?


## Wording: Ordering of Questions

- "How often do you normally go out on a date? about $\qquad$ times a month."
- "How happy are you with life in general?"
- Strong association between these questions.
- If the ordering is reversed, then there would be no strong association between these questions



## Wording: Unnecessary Complexity

- "Do you sometimes find that you have arguments with your family members and co-workers?"
- Arguments with family members
- Arguments with co-workers



## Inferences about the Population

- Values calculated from samples are used to make conclusions (inferences) about unknown values in the population
- Variability
- different samples from the same population may yield different results for a particular value of interest
- estimates from random samples will be closer to the true values in the population if the samples are larger
- how close the estimates will likely be to the true values can be calculated -- this is called the margin of error


