

8.16. Let $\mathcal{F}_n = \sigma(\{X_i\}_{i=1}^n)$ to find that

$$\mathbf{E} \left[\prod_{i=1}^{n+1} \frac{g(X_i)}{f(X_i)} \mid \mathcal{F}_n \right] = \prod_{i=1}^n \frac{g(X_i)}{f(X_i)} \cdot \mathbf{E} \left[\frac{g(X_{n+1})}{f(X_{n+1})} \right] \quad \text{a.s.}$$

But $\mathbf{E}[(g/f)(X_{n+1})] = \int_{-\infty}^{\infty} (g/f)(x)f(x) dx = \int_{-\infty}^{\infty} g(x) dx = 1$. This has the desired result.