

Best ch 4 problem

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4.2
#28

The rain drop evaporates out ~~2~~ ~~times~~ two ~~times~~ the surface volume.

$$V = \frac{4}{3}\pi r^3$$

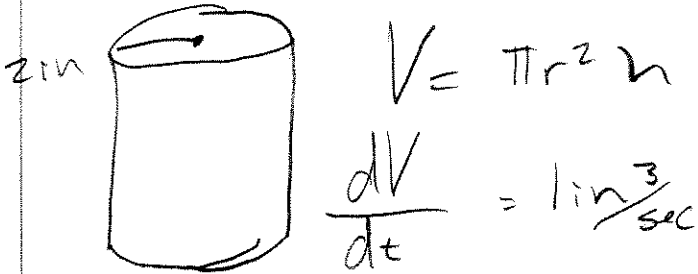
$$\frac{dV}{dt} = 4\pi r^2 \frac{dr}{dt}$$

$$\frac{dV}{dt} = -2$$

evaporation rate $\frac{dV}{dt} = -8\pi r^2$

This is a good problem b/c it is a ~~easy~~ easy to see implicit differentiation problem. To begin with we are trying to find the rate of change for volume, well it so happens that $\frac{dV}{dt} = \text{Surface area}$. Using a little bit of ~~thought~~ ~~app~~ ~~thought~~ thought evaporation is minus and equals $\frac{dV}{dt} = -2$. It helps to understand the theory when you can see it clearly in a problem.

4.2 #23 How fast does the level of a coke go down if you drink a cubic inch per second? The cup is a cylinder of radius 2 inches - first write down the volume



$$\frac{V(\text{in}^3)}{\pi(4 \text{ in}^2)} = h \rightarrow$$

$$\frac{dV}{dt} (1 \text{ in}^3/\text{sec})$$

$$\frac{-1}{\pi 4} =$$

$$-0.07958 \text{ in/sec}$$

is the change in h over the change in time

$$\frac{dh}{dt}$$

CH 4 Review Problem

CH 4 Sec 4.2 # 24

Question

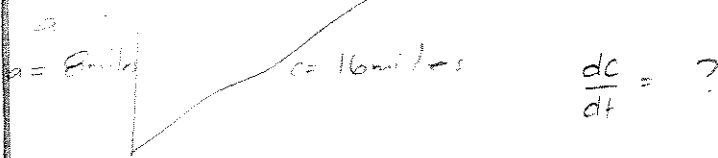
A jet flies at 8 miles up and 560 miles/hr.
 How fast is it approaching you when

a. It is 16 miles from you

b. Its shadow is 8 miles from you
 (sun is overhead)

c. The plane is 8 miles from you (exactly above)
 $db/dt = 560 \text{ miles/hr}$

Solution



To get c's distance:

$$a^2 + b^2 = c^2$$

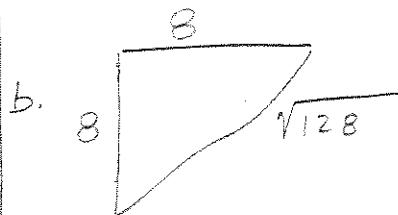
$$\sqrt{64 + b^2} = c$$

$$\text{Rate of distance} = \frac{b}{\sqrt{64 + b^2}} \frac{db}{dt} = \frac{dc}{dt}$$

c's rate when $c = 16 \text{ miles}$

$$b = \sqrt{16^2 - 8^2} \rightarrow \sqrt{256 - 64} = 8\sqrt{3}$$

$$\text{Therefore, } \frac{dc}{dt} = \frac{8\sqrt{3}}{16} (560) = \boxed{280\sqrt{3} \text{ miles/hour}}$$



c's rate when $c = \sqrt{128}$

$$\frac{dc}{dt} = \frac{8}{\sqrt{128}} (560) = \boxed{280\sqrt{2} \text{ miles/hour}}$$

c. 3
 If $c = 0$ then rate $\frac{dc}{dt} = 0$

(1) ...

5.4.10

$$\int \sqrt{1-3x} dx$$

$$u = 1-3x$$

$$du = -3 dx$$

$$-\frac{du}{3} = dx$$

$$\int \sqrt{u} \left(-\frac{du}{3}\right)$$

$$-\frac{1}{3} \int \sqrt{u} du$$

$$-\frac{1}{3} \int u^{1/2} du$$

$$-\frac{1}{3} \left(\frac{2}{3} u^{3/2}\right) + C$$

$$\left[-\frac{2}{9} (1-3x)^{3/2} + C\right]$$